

Tutorial - 1(D) Applications of Definite Integral

- Volume by slicing method :

1. Find the volume of a solid ball of radius a using slicing method.
2. Find the volume of a cone with height 4 c.m. using by slicing method.
3. Using slicing method, find the volume of solid obtained by rotating about the x-axis the region under the curve $y = \sqrt{2x}$ from 0 to 1.

- Volume by Rotation :

4. The Region between the curve $y = \sqrt{x}$, $0 \leq x \leq 4$ and x-axis is revolved about the x-axis to generate a solid. Find its volume.
5. Find the volume generated by revolving the area bounded by the parabola $y^2 = 8x$ and its latus rectum about y-axis.
6. Find the volume generated by revolving the area bounded by $2x = x^2, x = 4, y = 0$ about x-axis.
7. Find the volume of solid generated by revolving the cardioid $r = a(1 + \cos \theta)$ about the initial line.
8. Find the volume generated by revolving the arc bounded by the parabola $y^2 = 4ax$, $a > 0$ and latus rectum about latus rectum.

- Volume by Cylindrical Shells.

9. Find the volume generated by revolving the area bounded by $2y = x^2, x = 4, y = 0$ about y-axis
10. Find the volume of solid generated by rotating about y-axis and the region bounded by the curve $y = x$ and $y = x^2$.

11. Using cylindrical shells, find the volume of the solid obtained by rotating about the x -axis the region under the curve $y = \sqrt{x}$ from 0 to 1 .
12. Find the volume of the solid obtained about the line $y = -1$ the region bounded by the curves $y = x^2$ and $x = y^2$.